and monochromatization was not sufficient. Recalculation based on only the low-order reflections with $\sin \theta / \lambda \leq 0.6 \AA^{-1}$ gave $R(F) 0.028$ for 110 unique reflections and $w R(F)=0.035$.* Equivalent isotropic thermal parameters, $B_{\text {eq }}$, for $\mathrm{Pt}, \mathrm{Cl}$ and K decreased from $2.22(10), 2.89(6)$ and $3.33(24) \AA^{2}$ to $1.83(10)$, 2.49 (6) and 2.92 (21) $\AA^{2}$, respectively and approached the X-ray values, $1.69(1), 2.47(2)$ and $2.85(3) \AA^{2}$.

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> * See deposition footnote.

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# Preparation and Structure of the Aluminium Ammonium Phosphate Dihydrate $\mathrm{Al}_{2}\left[\mathrm{NH}_{4}\right](\mathrm{OH})\left(\mathrm{PO}_{4}\right)_{2} \cdot \mathbf{2} \mathrm{H}_{2} \mathrm{O}$ :* A Tunnel Structure with Ammonium Ions in the Channels 

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#### Abstract

M_{r}=315 \cdot 0\), monoclinic, $\quad P 2_{1} / n, \quad a=$ 9.553 (1), $\quad b=9.577(1), \quad c=9.614$ (1) $\AA, \quad \beta=$ $103.56(1)^{\circ}, V=855.1 \AA^{3}, Z=4, D_{x}=2.45 \mathrm{~g} \mathrm{~cm}^{-3}$, $\lambda($ Mo $K \alpha)=0.7107 \AA, \quad \mu=6.4 \mathrm{~cm}^{-1}, \quad F(000)=640$, $T=293$ K. Final $R=0.025$ for 2449 observed data. The structure is isomorphous with $\mathrm{GaPO}_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ with columns of Al-centred corner- and edge-shared octahedra linked via $\mathrm{PO}_{4}$ tetrahedra to outline channels approximately parallel to the $b$ axis. Ammonium groups occupy these channels and are hydrogen-bonded to framework O atoms and water molecules.


Introduction. Aluminium phosphate hydrates with $\mathrm{Al} / \mathrm{P}=1.0$ have been reported as the minerals variscite (Kniep, Mootz \& Vegas, 1977) and metavariscite

[^0]0108-2701/84/101641-03\$01.50
(Kniep \& Mootz, 1973). In these structures P and Al are in tetrahedral and octahedral coordination respectively. Recently a new class of molecular sieves constructed by a network of corner-shared $\mathrm{AlO}_{4}$ and $\mathrm{PO}_{4}$ tetrahedra has been described and one of these phases has had its structure determined from singlecrystal X-ray data (Wilson, Lok \& Flanigen, 1982; Wilson, Lok, Messina, Cannan \& Flanigen, 1982). It was during the attempted synthesis of the aluminium phosphate molecular sieve, $\mathrm{AlPO}_{4}-14$ (Wilson, Lok \& Flanigen, 1982), that a new structure type for $\mathrm{AlPO}_{4}$ was synthesized. In this structure Al is in an octahedrally coordinated site thereby relating it to variscite and metavariscite.

Subsequent to the determination of the structure of the compound reported here it was found to be isomorphous with $\mathrm{GaPO}_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ (Mooney-Slater, (c) 1984 International Union of Crystallography

Table 1. Fractional atomic coordinates ( $\times 10^{4}$, for H $\times 10^{3}$ ) and isotropic thermal parameters $\left(\times 10^{4}\right.$, for H $\times 10^{3}$ ) with e.s.d.'s in parentheses

|  | $x$ | $y$ | $z$ | $U_{\mathrm{eq}}{ }^{*} / U\left(\AA^{2}\right)$ |
| :--- | ---: | ---: | ---: | ---: |
| $\mathrm{P}(1)$ | $1985(1)$ | $5319(1)$ | $3482(1)$ | $50(1)$ |
| $\mathrm{P}(2)$ | $2947(1)$ | $1921(1)$ | $6368(1)$ | $50(1)$ |
| $\mathrm{Al}(1)$ | $1138(1)$ | $4629(1)$ | $6280(1)$ | $57(1)$ |
| $\mathrm{Al}(2)$ | $1074(1)$ | $2291(1)$ | $3150(1)$ | $55(1)$ |
| $\mathrm{O}(1)$ | $2099(1)$ | $3859(1)$ | $2847(1)$ | $80(2)$ |
| $\mathrm{O}(2)$ | $2369(1)$ | $5200(1)$ | $5132(1)$ | $77(2)$ |
| $\mathrm{O}(3)$ | $2083(1)$ | $3017(1)$ | $6966(1)$ | $93(2)$ |
| $\mathrm{O}(4)$ | $432(1)$ | $5859(1)$ | $2966(1)$ | $74(2)$ |
| $\mathrm{O}(5)$ | $2205(1)$ | $5516(1)$ | $7899(1)$ | $74(2)$ |
| $\mathrm{O}(6)$ | $2392(1)$ | $1758(1)$ | $4762(1)$ | $87(2)$ |
| $\mathrm{O}(7)$ | $3068(1)$ | $6274(1)$ | $3052(1)$ | $91(2)$ |
| $\mathrm{O}(8)$ | $-462(1)$ | $2678(1)$ | $1658(1)$ | $89(2)$ |
| $\mathrm{OW}(1)$ | $-34(1)$ | $6352(1)$ | $5542(1)$ | $78(2)$ |
| $\mathrm{OW}(2)$ | $1(2)$ | $9327(2)$ | $6466(2)$ | $139(3)$ |
| $\mathrm{O} W(3)$ | $1828(2)$ | $8565(2)$ | $4623(2)$ | $207(4)$ |
| N | $-135(2)$ | $-1904(2)$ | $1040(2)$ | $163(3)$ |
| $\mathrm{H}(1)$ | $44(3)$ | $687(3)$ | $526(3)$ | $21(7)$ |
| $\mathrm{H}(2)$ | $-40(3)$ | $1002(3)$ | $604(3)$ | $32(6)$ |
| $\mathrm{H}(3)$ | $73(4)$ | $958(3)$ | $675(3)$ | $36(9)$ |
| $\mathrm{H}(4)$ | $224(4)$ | $854(4)$ | $393(5)$ | $66(12)$ |
| $\mathrm{H}(5)$ | $234(5)$ | $914(4)$ | $537(5)$ | $53(8)$ |
| $\mathrm{H}(6)$ | $-90(4)$ | $-140(4)$ | $95(4)$ | $44(7)$ |
| $\mathrm{H}(7)$ | $-8(4)$ | $-261(4)$ | $155(4)$ | $39(7)$ |
| $\mathrm{H}(8)$ | $58(4)$ | $-144(3)$ | $143(3)$ | $37(7)$ |
| $\mathrm{H}(9)$ | $-4(4)$ | $-213(4)$ | $21(4)$ | $84(12)$ |

${ }^{*} U_{\mathrm{eq}}=\frac{1}{3}\left(U_{11}+U_{22}+U_{33}\right)$ for all non-H atoms: e.s.d.'s according to Schomaker \& Marsh (1983).
1966). The study was used as an opportunity to understand the details of the hydrogen-bonding scheme and, by inference, of that in $\mathrm{GaPO}_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ in which H atoms were not located.

Experimental. The starting mixture for an $\mathrm{AlPO}_{4}-14$ preparation (Wilson, Lok \& Flanigen, 1982) was sealed in a thick-walled Pyrex-glass capsule and heated at 423 K for 24 h . Clear crystal, $0.15 \times 0.08 \times 0.08 \mathrm{~mm}$. Weissenberg and precession photographs indicated monoclinic ( $2 / m$ ) symmetry, space group $P 2_{1} / n$ (No. 14) with absences: $h 0 l, h+l=2 n+1 ; 0 k 0, k=$ $2 n+1$. Cell parameters determined from 12 high-angle ( $56<2 \theta<60^{\circ}$ ) centred reflections. Picker FACS-I diffractometer, pyrolytic-graphite monochromator; intensities measured to $\theta=30^{\circ}$ with 20 s fixed background counting times; range of $h k l: h-13 \rightarrow 13, k$ $0 \rightarrow 13, l 0 \rightarrow 13$; three standard reflections monitored periodically showed no significant variation; 64 of 2513 reflections measured had $I \leq 0.0$ and were excluded from structure solution or refinement; 2449 intensities corrected for Lorentz and polarization effects, no absorption correction applied ( $\mu R \simeq 0 \cdot 1$ ); structure solved using automatic centrosymmetric direct-methods routine of SHELX76 (Sheldrick, 1976) to find $\mathrm{AlPO}_{4}$ framework; difference Fourier techniques to find OW, N and H positions; atomic parameters refined using full-matrix least squares; function minimized $\sum w\left(F_{o}-\right.$ $\left.F_{c}\right)^{2}$, weights given as $\sigma^{-2}(F) ; \sigma$ is based on the $\sigma_{2}$ weights described by Busing \& Levy (1957), $\sigma_{2}$ $=\left[\left(\sigma_{1} / \mathrm{Lp}\right)^{2}+(\mathrm{PSQ}) F_{o}^{4} / 2-\left.F_{o}\right|^{1 / 2}\right.$ where $\sigma_{1}$ is based on
counting statistics, Lp is the Lorentz-polarization factor and PSQ is the instrumental uncertainty factor ( $=0.002$ ). The $\sigma_{2}$ scheme tends to down-weight the very intense reflections in the data set. Three 'water' positions [numbered $\mathrm{O} W(1)$ through $\mathrm{O} W(3)$ ] located. Final refinement employed fixed occupancies, anisotropic non-H atoms, isotropic H ; max. peak in final difference map 0.5 e $\AA^{-3}, 0.9 \AA$ from P -atom sites. There were smaller peaks $\left(0.3 \mathrm{e} \AA^{-3}\right.$ ) within $1.2 \AA$ of N perhaps indicating a greater degree of disorder for the $\left[\mathrm{NH}_{4}\right]^{+}$species. Inclusion of these positions ( $0 \cdot 02$, $-0.23,0.19$ and $0.0,-0.26,0.03$ ) in the least-squares refinement did not improve the $R$ value; a common isotropic thermal parameter refined for the five sites converged to a negative value. A model of four H atoms was accepted as being most consistent with the observed diffraction data.

Analytical expressions for the scattering factors those of Sheldrick (1976) excepting that for Al which was taken from International Tables for X-ray Crystallography (1974); anomalous-dispersion correction included; final discrepancy factors (Sheldrick, 1976) $R=0.025$ and $R_{w}=0.030$ for all data with $I>0 ;$ $(\Delta / \sigma)_{\max }=0 \cdot 2$. All calculations carried out on ANU Univac 1100 computer; major programs used: SHELX76 (Sheldrick, 1976) and ORTEP (Johnson, 1965).

Discussion. Final atomic parameters are given in Table 1.*

The structure of the $\mathrm{AlPO}_{4}$ framework is essentially as described by Mooney-Slater (1966) for $\mathrm{GaPO}_{4}$.$2 \mathrm{H}_{2} \mathrm{O}$. However, H positions, located in the analysis of this structure, give a more complete picture of the hydrogen bonding between water molecules and hydroxyl species attached to Al and the ammonium group. $\left|\mathrm{NH}_{4}\right|^{+}$, which occupies the channels formed by the $\left|\mathrm{Al}_{2}(\mathrm{OH})\left(\mathrm{PO}_{4}\right)_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}\right|$ framework (Fig. 1).

[^1]

Fig. 1. Stereoscopic drawing (Johnson. 1965) of the structure viewed down the $b$-axial direction. H atoms have been given arbitrary radii. The $\left|\mathrm{NH}_{4}\right|^{+}$groups occupy the channel formed by Al-centred octahedra and P-centred tetrahedra.

Selected interatomic distances and angles are given in Table 2 and drawings of the individual environments for 'water' are given in Fig. 2.

Table 2. Selected interatomic distances ( $\AA$ ) and angles $\left({ }^{\circ}\right)$ with e.s.d.'s in parentheses

| $\mathrm{P}(1)-\mathrm{O}(1) \quad 1$ | 1.540 (1) | $\mathrm{P}(2)-\mathrm{O}(3) \quad 1.5$ | 1.528 (1) |
| :---: | :---: | :---: | :---: |
| -O(2) 1 | 1.546 (1) | -O(5) 1.5 | 1.542 (1) |
| -O(4) 1 | 1.540 (1) | -O(6) 1.5 | 1.518 (1) |
| $-\mathrm{O}(7) \quad 1$ | 1.509 (1) | $-\mathrm{O}(8) \quad 1.5$ | 1.529 (1) |
| $\mathrm{O}(1)-\mathbf{P}(1)-\mathrm{O}(2)$ | 108.6 (1) | $\mathrm{O}(3)-\mathrm{P}(2)-\mathrm{O}(5)$ | 108.1 (1) |
| -O(4) | 109.2 (1) | -O(6) | 111.2 (1) |
| -O(7) | 108.9 (1) | -O(8) | 111.1 (1) |
| $\mathrm{O}(2)-\mathrm{P}(1)-\mathrm{O}(4)$ | 109.6 (1) | $\mathrm{O}(5)-\mathrm{P}(2)-\mathrm{O}(6)$ | 109.1 (1) |
| -O(7) | 108.2 (1) | -O(8) | 109.4 (1) |
| $\mathrm{O}(4)-\mathrm{P}(1)-\mathrm{O}(7)$ | $112 \cdot 2$ (1) | $\mathrm{O}(6)-\mathrm{P}(2)-\mathrm{O}(8)$ | $107 \cdot 9$ (1) |
| $\mathrm{Al}(1)-\mathrm{O}(2) \quad 1$ | 1.873 (1) | $\mathrm{Al}(2)-\mathrm{O}(1) \quad 1.85$ | 1.853 (1) |
| -O(3) 1 | 1.831 (1) | -O(6) 1.82 | 1.826 (1) |
| -O(4) 1 | 1.872 (1) | -O(8) 1.83 | 1.833 (1) |
| -O(5) 1 | 1.855 (1) | -O(7) 1.8 | 1.845 (1) |
| -0W(1) 2 | 2.027 (1) | -OW(2) 1.9 | 1.942 (1) |
| $-\mathrm{OW}(1) \quad 2$ | 2.048 (1) | -OW(1) $2 \cdot 2$ | 2.201 (1) |
| $\mathrm{O}(2)-\mathrm{Al}(1)-\mathrm{O}(3)$ | 97.7 (1) | $\mathrm{O}(1)-\mathrm{Al}(2)-\mathrm{O}(6)$ | 94.3 (1) |
| -O(4) | 166.4 (1) | -O(8) | 94.0 (1) |
| -O(5) | 93.6 (1) | -O(7) | 90.0 (1) |
| -OW(1) | ) $85.9(1)$ | -OW(2) | 178.0 (2) |
| $-\mathrm{O} W(1)$ | ) 84.2 (1) | $-\mathrm{OW}(\mathrm{1})$ | 86.4 (1) |
| $\mathrm{O}(3)-\mathrm{Al}(1)-\mathrm{O}(4)$ | 91.3 (1) | $\mathrm{O}(6)-\mathrm{Al}(2)-\mathrm{O}(8)$ | 170.7 (1) |
| -O(5) | 87.5 (1) | -O(7) | 93.7 (1) |
| -OW(1) | ) 176.1 (1) | -OW(2) | 84.6 (2) |
| -OW(1) | ) $91.9(1)$ | -OW(1) | 89.7 (2) |
| $\mathrm{O}(4)-\mathrm{Al}(1)-\mathrm{O}(5)$ | 97.0 (1) | $\mathrm{O}(8)-\mathrm{Al}(2)-\mathrm{O}(7)$ | 90.5 (1) |
| -OW(1) | ) 84.9 (1) | -OW(2) | 87.0 (2) |
| -OW(1) | ) 85.3(1) | -OW(1) | 86.7 (1) |
| $\mathrm{O}(5)-\mathrm{Al}(1)-\mathrm{O} W(1)$ | ) 94.1 (1) | $\mathrm{O}(7)-\mathrm{Al}(2)-\mathrm{O} W(2)$ | 91.7 (2) |
| -OW(1) | ) 177.6 (1) | -OW(1) | ) 175.3 (1) |
| $\mathrm{O} W(1)-\mathrm{Al}(1)-\mathrm{O} W($ | (1) $86.7(1)$ | $\mathrm{O} W(2)-\mathrm{Al}(2)-\mathrm{O} W(1)$ | (1) $91.9(2)$ |



Fig. 2. The unit cell viewed down the $b$-axial direction emphasizing the relationship between water and ammonium species. Hydrogen bonds are depicted as thin lines (see text).

The phosphate tetrahedra are only slightly distorted and the average $\mathrm{P}-\mathrm{O}$ distances $[1.53$ (2) and 1.53 (1) $\AA$ for $\mathrm{P}(1)$ and $\mathrm{P}(2)$ tetrahedra respectively] and angles [109 (1) ${ }^{\circ}$ ] are similar for those reported for the other $\mathrm{AlPO}_{4} .2 \mathrm{H}_{2} \mathrm{O}$ structures, variscite [1.53 (1) $\AA$ and $\left.109(2)^{\circ}\right]$ and metavariscite [1.53 (1) $\AA$ and $\left.109(1)^{\circ}\right]$ (Kniep \& Mootz, 1973; Kniep et al., 1977). The Al-centred octahedra are significantly distorted. Average bond lengths between Al and 'non-water' O atoms $[1.86$ (2) and $1.84(1) \AA$ for $\mathrm{Al}(1)$ and $\mathrm{Al}(2)$ octahedra respectively] are shorter than in variscite, 1.88 (2) $\AA$, and metavariscite, 1.88 (1) $\AA$, while the distance between Al atoms and 'water' O atoms is considerably longer (Table 2). The longest of these distances involves $\mathrm{O} W(1)$ which is 2.201 (1) $\AA$ from $\mathrm{Al}(2)$. This has the effect of distorting the $\left[\mathrm{AlO}_{3}-\right.$ $\left(\mathrm{H}_{2} \mathrm{O}\right) \mathrm{OH}$ ] octahedron towards a square-based pyramid. Angles are also distorted from the ideal with $\mathrm{O}(2)-\mathrm{Al}(1)-\mathrm{O}(4)=166.4(1)^{\circ}$ being the largest deviation. These distortions are more pronounced than those previously described in $\mathrm{GaPO}_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ (MooneySlater, 1966).

Fig. 2 illustrates the relationship between OH and $\mathrm{H}_{2} \mathrm{O}$ bound to the framework. $\mathrm{O} W(2)$ and $\mathrm{OW}(3)$ are hydrogen-bonded to one another [ $\mathrm{OW}(3) \cdots \mathrm{H}(2)-$ $\mathrm{O} W(2)]$ and to framework O atoms (Fig. 2). The ordered $\left[\mathrm{NH}_{4}\right]^{+}$group is hydrogen-bonded to four framework O atoms; those sites closest to O atoms are $\mathrm{H}(6)$ and $\mathrm{H}(7)$. There are two O atoms $[\mathrm{O} W(3)$ and $\mathrm{O}(4)$ ] at distances of 2.28 and $2.40 \AA$ respectively from $\mathrm{H}(1)$ suggesting that only weak hydrogen bonds exist between $\mathrm{H}(1)$ and these atoms. The accepted hydrogen bonds have O (or N ) -H 0.73 (4)-0.94 (5), $\mathrm{H} \cdots \mathrm{O}$ 1.93 (3)-2.2 (3), O(or N) ...O 2.713 (3)-2.998 (3) A, and $\mathrm{O}($ or N$)-\mathrm{H} \cdots \mathrm{O} 152(5)-172$ (4) ${ }^{\circ}$.

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[^0]:    * Dialuminium ammonium hydroxide bis(orthophosphate).

[^1]:    * Lists of structure factors, anisotropic thermal parameters and geometry for the hydrogen bonds have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 39518 (18 pp.). Copies may be obtained through The Executive Secretary. International Union of Crystallography. 5 Abbey Square. Chester CH1 2HU. England.

